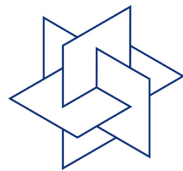


# Pen-based Input of Geometric Constructions

Dirk Materlik, Ulrich Kortenkamp



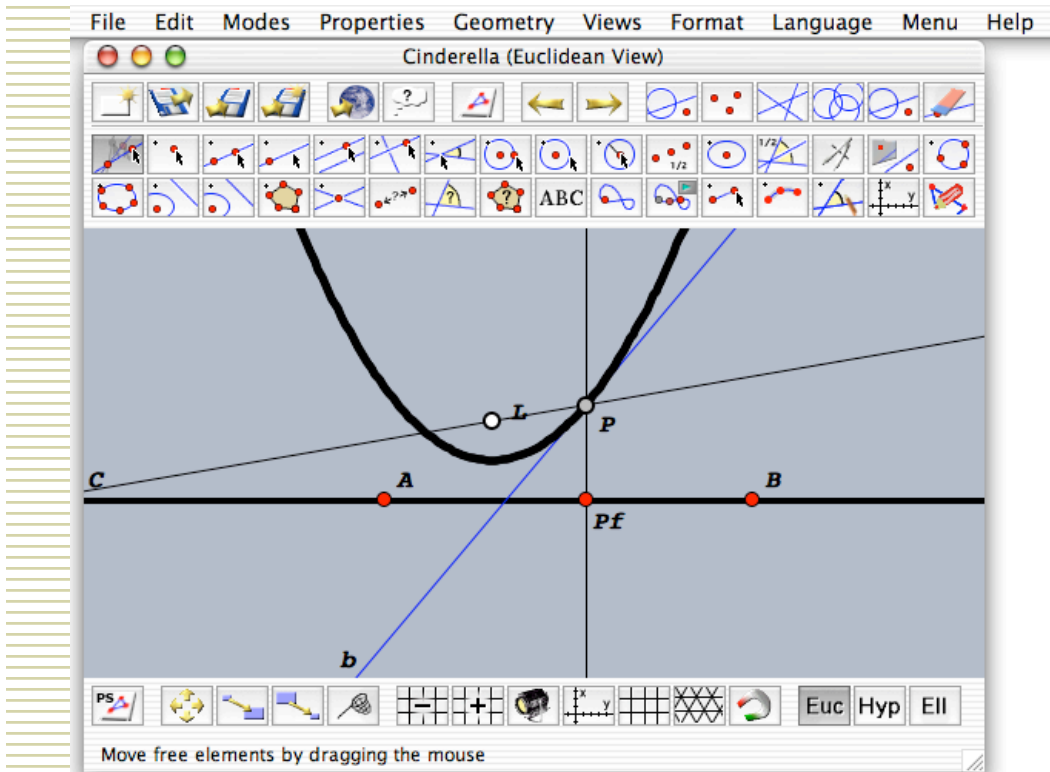
DFG Research Center Matheon  
“Mathematics for key technologies”



Technical University Berlin



# Cinderella



- ◆ Dynamic Geometry
- ◆ Advanced Mathematics
- ◆ Written in Java
- ◆ Target platform: standard computers

# Interactive Whiteboards

- ◆ Large
- ◆ High Resolution
- ◆ Special Pen
  - Pointer at pen position
  - Two buttons
- ◆ Acts as a mouse
- ◆ Normal computer





# Pen-driven devices

- ◆ Interactive Whiteboards
- ◆ PDAs
- ◆ Graphics Tablets
- ◆ Tablet PCs

# Common properties

- ◆ Logical movement by physical movement
- ◆ Classical User Interface is problematic
  - Large movements awkward
  - Exact pointing more difficult
  - Multiple windows confusing

**Goal: Use like pen and paper.**

**→Eliminate modes!**



– Demo –













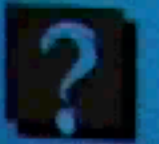



*Triangle*

*Intersection of perpendicular bisectors*

*Circle through vertices*

*Moving*

Applications Settings Files

 EMail	 NetFront v3.0	 Music Player	 Movie Player
 Media Player	 Presentation	 ImagePad	 Voice Recorder
 Terminal	 Calculator	 City Time	 Clock
 Help Browser	 Cinderella	 FreeNote0t	 Jisho

あ 11:25



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# Scribbling Capabilities

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## ◆ Create

- Points
- Lines
- Circles
- Polylines

## ◆ Modify

- Select
- Move
- Undo / Redo
- Edit Label
- Inspect
- Right click



# Annotations vs. Preselections

- ◆ Problem: Recognize dependant objects

- Easy for “Point on Line” etc.
- Hard for “Orthogonal”, “Midpoint” etc.

- ◆ Approaches

- Preselections
- Annotations – Demo –

*ScribbleJ* Orthogonals /  
Parallels



# Annotations

## ◆ Advantages

- More “natural” gesture
- Can be done as an afterthought

## ◆ Problems

- Not possible for every element
- Aggravated by Undo/Redo-Facilities
- Needs many gestures



# Preselections

## ◆ Advantages

- Simple concept that can be applied everywhere
- Modify meaning of gestures
- Exact
- Less false positives

## ◆ Disadvantages

- User has to decide in advance

# “Hand-drawn” presentation

- ◆ Do not correct the user
- ◆ But relations have to be right

– Demo –

- *Pappos’ Theorem*
- *Circumference again*
- *Incremental Smoothing*

# Timeline

- ◆ Incorporated into Cinderella 2.0
- ◆ Now: Beta-Version
  - Regular version
  - PDA
- ◆ Future directions
  - Physics (prototype available)
  - More devices
  - More gestures, more recognized objects

To become a beta tester:  
[materlik@math.tu-berlin.de](mailto:materlik@math.tu-berlin.de)



# Design goals

- ◆ ~~Intuitive~~ Easy To Learn
- ◆ Fast to use
- ◆ Natural with a pen
- ◆ Flexible
- ◆ Anticipate future hardware developments
- ◆ Alleviate need for modes and menus



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# Conclusion

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- ◆ It is feasible to recognize mathematical entities from user-drawn sketches
- ◆ In real-time
- ◆ On small and large devices
- ◆ Hand-drawn appearance can be preserved
  
- ◆ Mathematical knowledge in the kernel enables these possibilities



# Done.

- ◆ Questions?

- ◆ More Demos?

- *Physics*
- *Flow Menus*
- *Scribbled Cube*
- *Scribbled Euler-Line*